

## NUMERICAL SOLUTIONS OF THE DISSIPATIVE NONLINEAR SCHRÖDINGER EQUATION WITH VARIABLE COEFFICIENT ARISES IN ELASTIC TUBE

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**Abstract.** In this paper, we solved the dissipative nonlinear Schrödinger Equation (DNLSV) with variable coefficient by Crank-Nicolson (CN) implicit finite-difference method. The DNLSV equation arises in nonlinear wave modulation in an elastic tube with a symmetrical stenosis filled with viscous fluid. We then compared numerical solutions with its progressive wave solution. The CN scheme is consistent with the differential equation and is unconditionally stable.

**Keywords.** dissipative, nonlinear Schrödinger Equation, Crank-Nicolson, finite-difference method, progressive wave solution

**AMS (MOS) subject classification:** 65N40

## 1 Introduction

The studies in [1] - [2] have investigated a weakly nonlinear wave modulation in a prestressed fluid-filled stenosed elastic tube filled with a Newtonian fluid where approximate viscous fluid equations without boundary conditions were used, while similar studies but viscous equations with boundary conditions were used have been examined in [1] and [3]. Then, by applying the reductive perturbation method in long wave approximation, stretched coordinate of boundary-value type and extending the field quantities into the asymptotic series of order  $\epsilon$  where  $\epsilon$  is a small parameter, the governing equations in [1] -