

## BEHAVIOR OF TWO AND THREE-DIMENSIONAL SYSTEMS OF DIFFERENCE EQUATIONS IN MODELLING COMPETITIVE POPULATIONS

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**Abstract.** The main objective of this paper is to determine the closed form solutions of system of non-linear difference equations in the modelling competitive populations

$$x_{n+1} = \frac{x_{n-1}}{a_n + x_{n-1} y_n}, y_{n+1} = \frac{y_{n-1}}{a_n + y_{n-1} x_n}, z_{n+1} = \frac{1}{y_n z_n}$$

where  $\{a_n\}$  sequence with initial values  $x_{-1}, x_0, y_{-1}, y_0,$  and  $z_0$  such that  $x_{-1} y_0 \neq -a_0, x_0 y_1 \neq -a_1, y_{-1} x_0 \neq -a_0, ,$  and  $y_0 x_1 \neq -a_1$ . We study some special cases of system (1). In the Final section ,we introduce numerical examples.

**Keywords.** solutions, difference equation, competitive, convergence, stability

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### 1 Introduction

Discrete dynamical systems or Difference equations [35] is varied field which manipulate nearly every offshoot of applied and pure mathematics. The studying of properties of systems of difference equations is a subject of interest in last years, see books [[1], [11], [17]]. A difference equations system of order one

$$S_{n+1} = \phi(S_n, T_n) \quad , \quad T_{n+1} = \psi(S_n, T_n) \quad (1)$$

,  $n = 0, 1, \dots, (S_0, T_0) \in R$  ,  $R$  subset of  $\mathbb{R}^2, (\phi, \psi) : R \rightarrow R$ , and  $\phi, \psi$  are mapping is *competitive* if  $\phi(s, t)$  is non-decreasing in  $s$  and non-increasing in  $t$ ; and  $\psi(s, t)$  is nondecreasing in  $t$  and nonincreasing in  $s$  [36].

Competitive systems deliberated by plentiful authors (For examples [3], [4], [8], [15], [18], [26], [36] , [37], [38]).

In a modelling framework, competitive system of nonn-linear difference equations

$$s_{n+1} = \frac{s_n}{a + t_n} \quad \& \quad t_{n+1} = \frac{t_n}{b + s_n}$$