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## FIRST ORDER THRESHOLD INTEGER-VALUED MOVING AVERAGE PROCESSES

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**Abstract.** In this paper, we introduce a new threshold model with poisson innovation: Threshold Integer-Valued Moving Average model (TINMA). We derive the numerical characteristics of TINMA(1) model. Stationary and ergodicity are also obtained. The methods of estimation under analysis is Yule-Walker. Some simulation results illustrate the performance of the proposed method.

Keywords. INMA; Threshold; Stationary; Ergodicity; Poisson.

AMS (MOS) subject classification: 37M10, 62M10.

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