

## NOTE OF A THEOREM IN SINGULARITY THEORY

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**Abstract.** Our algorithm for solving the recognition problem in bifurcation theory splits monomials into three classes: low-order terms, intermediate-order terms and higher-order terms. In describing the low-order terms, 'the smallest intrinsic ideal containing a germ  $h'$  is introduced by Golubitsky M and Schaeffer D G, then they give a proposition, but the proof of the proposition is not right. In this paper we prove the proposition again.

**Keywords.** bifurcation; codimension; intrinsic ideal; equivalence.

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