

**MIN-MAX SOLUTIONS FOR THE IMPULSIVE
BOUNDARY VALUE PROBLEMS FOR THE
 $(P_1(T), P_2(T))$ -LAPLACIAN SYSTEMS**

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Abstract. In this work we investigate via Ky Fan's inequality the existence of solutions to impulsive problems with the $(p_1(t), p_2(t))$ -Laplacian systems and Dirichlet boundary value conditions.

Keywords. *critical point theory; Ky-Fan inequality; saddle point solution.*

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