

EXISTENCE RESULTS ON IMPULSIVE STOCHASTIC FUNCTIONAL DIFFERENTIAL INCLUSIONS WITH DELAYS

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Abstract. This article presents the results on existence of mild solutions for impulsive stochastic differential inclusions under sufficient conditions. The results are obtained by using the Dhage's fixed point theorem.

Keywords. multivalued map, existence, impulsive stochastic differential inclusions, fixed point theorem.

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