

SMOOTHNESS PROPERTY ON PARAMETERS OF SOLUTIONS OF CAUCHY PROBLEMS WITH NON-DENSELY DEFINED OPERATORS

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Abstract. This work investigates the differentiability with respect to parameters of the classical solutions of abstract Cauchy problems, and studies the case that the operators of the equations are not densely defined by employing the theory of integrated semigroup.

Keywords. abstract Cauchy problem, integrated Semigroup, differentiability, parameter, classical solution

AMS (MOS) subject classification: 47D62, 34A30.

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