

## ON-OFF ATTITUDE CONTROL USING PULSE-WIDTH PULSE-FREQUENCY MODULATED INPUT SHAPER

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**Abstract.** Kinetic kill vehicle (KKV) is actuated by on-off thrusters to adjust its attitude, how to modulate continuous control commands to on-off or pulse signals to meet the requirements of the thrusters is a challenging task. Pulse-width pulse-frequency (P-WPF) modulation is an effective method that provides pseudolinear operation for on-off thrusters. In this work, a new thruster configuration of the KKV and its mathematical model is proposed, good guidelines for the P-WPF parameters tuning task is presented, the linear quadratic regulator (LQR) technique in combination with P-WPF is used to design the optimal attitude controller. The validity of the proposed methods is demonstrated through the three-axis nonlinear numerical simulations of the KKV of this work.

**Keywords.** Attitude control; KKV; LQR; Optimal control; P-WPF.

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