

## MINIMAX FRACTIONAL INTEGRAL PROGRAMMING PROBLEMS INVOLVING UNIVEXITY

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**Abstract.** In this paper, we consider the problem that consists of minimizing a maximum of several time dependent ratios involving integral expressions. We establish optimality conditions based on the generalized univexity. Furthermore, we explore the Wolfe type dual model, Mond-Weir type dual model, one parameter dual model and Mixed type dual model, and then establish weak, strong and strict converse duality theorems under generalized univexity conditions.

**Keywords.** Nondifferentiable fractional variational programming; Invexity; Quasiinvexity Pseudoinvexity; Duality.

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### 1 Introduction

Fractional programming is one of the most application-enhanced areas of optimization which features in several types of practical problems. It can be applied to different branches of engineering as well as to economics to minimize a ratio of functions between given periods of time. Furthermore it can be utilized as a resource in order to measure the efficiency or productivity of a system. In such type of problems the objective function is given as a ratio of functions (see Stancu-Minasian [10]).

In the present paper, we consider a problem that deals with minimizing a maximum of several time dependent ratios involving integral expressions. Several researchers have investigated this type of problem, including Chen and Lai [2], Chandra et al. [1], Craven [3], Crouzeix et al. [4], Lee and Lai [7], Mond et al. [8], and Mond and Husain [9], while we extend the results of Lai [5] and Lai and Liu [6] to the case of the generalized univexity. As our problem involves a state function  $x(t)$  in the integrand of the integration, the obtained results also relate to the problems on optimal control. For more details, we refer the reader [11-13].