

A PONTRYAGIN PRINCIPLE FOR INFINITE-HORIZON PROBLEMS UNDER CONSTRAINTS

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Abstract. We establish a new Pontryagin principle for discrete-time infinite-horizon Optimal Control problems when the control variable depends on the state variable. Our methods use a reduction to finite-horizon problems.

Keywords. Pontryagin principle, infinite horizon, difference equation, difference inequation, optimal control,

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