

## GLOBAL ROBUST OUTPUT REGULATION WITH GENERALIZED IMMERSION

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**Abstract.** The global robust output regulation problem is solved in this paper for classes of nonlinear systems that do not satisfy the standard conditions for the existence of a linear internal model, but admit a so-called “generalized immersion.” It is shown how the obstacle given by the presence of the exosystem dynamics in the generalized immersion mapping or the necessity to construct a nonlinear internal model can be overcome by resorting to a recently developed framework for time-varying adaptive internal model design.

**Keywords.** Nonlinear Systems, Output Regulation, Internal Model, System Immersion, Adaptive Control.

**AMS (MOS) subject classification:** 93B52, 93C10, 93C40, 93D15, 93D21.

### 1 Introduction

Among many a fundamental contribution given by Prof. Hassan Khalil to the discipline of nonlinear control theory, his work on the nonlinear servomechanism problem stands out as a true milestone, marking the emergence of a methodology for non-local robust nonlinear regulation that has shaped the field for at least a decade. In a series of papers [17, 18, 20, 21] Khalil and co-workers, building on their newly developed method for robust stabilization by dynamic output feedback [10, 19], significantly extended the state of the art by providing the first systematic design of servocompensators achieving semi-global regulation by error feedback for nonlinear plant models characterized by large parametric uncertainty. Khalil was among the first to realize, together with Delli Priscoli [6] and Huang and Lin [13], that in order to provide robustness against parameter variations, the internal model incorporated in the controller must be able to produce, together with the trajectories of the exosystem, a certain number of higher harmonics. The ideas developed in this series of papers proved to have a longstanding influence, and are still found, in different shapes, in the most recent contribution to the field.