

The Existence of Solutions for the Nonlinear First Order Fuzzy Differential Equations with Discontinuous Conditions

Yeol Je Cho¹ and Heng-You Lan²

¹Department of Mathematics Education
and the RINS College of Education
Gyeongsang National University
Chinju 660-701, Korea

E-mail: yjcho@gsnu.ac.kr

²Department of Mathematics
Sichuan University of Science & Engineering
Zigong, Sichuan 643000, P. R. China

Abstract. In this paper, by using the directional Lipschitzian condition and Krasnosel'skii's fixed point theorem, we obtain some new existence theorems of solutions for a class of initial value problems of nonlinear first order fuzzy differential equations in the metric space of normal fuzzy convex sets with distance given by maximum of the Hausdorff distance between level sets.

Key Words: Nonlinear first-order fuzzy differential equation; initial value problem; directional Lipschitzian condition and fixed point; existence.

AMS (MOS) Subject Classification: 2000 Mathematics Subject Classification: 34A10; 26E50; 47E05.

1 Introduction

In this paper, we study the following initial value problem of fuzzy differential equation: Find $x : J \rightarrow E^n$ such that

$$\begin{cases} x'(t) = f(t, \lambda x(t)) + g(t, x(t)), \\ x(t_0) = x_0, \end{cases} \quad (1)$$

where $J = [t_0, t_0 + a] \subset R = (-\infty, +\infty)$ is a compact interval, E^n is the family of all fuzzy sets $u : R^n \rightarrow [0, 1]$, $t_0 \in R$, $x_0 \in E^n$, $f, g : W \rightarrow E^n$ are two nonlinear functions, $W = J \times B_b(x_0)$, $a, b \in R^+ = (0, +\infty)$, $B_r(\omega)$ denotes the ball which center at ω and radius is r and $\lambda > 0$ is a constant.

¹The first author was supported by the Korea Research Foundation Grant (KRF-2003-005-C00013) and the second author was supported from the Educational Science Foundation of Sichuan Province, China (2004C018).

²The corresponding author: hengyoulan@163.com (Heng-you Lan).