

# GLOBAL EXPONENTIAL STABILITY OF TIME-VARYING DELAY NEURAL NETWORKS VIA RAZUMIKHIN TECHNIQUE <sup>†</sup>

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**Abstract.** By employing Razumikhin technique, this paper establishes some Razumikhin type theorems for globally exponential stability of functional differential systems. It then presents, based on these Razumikhin-type theorems, some delay-independent and delay-dependent algebraic criteria for global exponential stability of time-varying delay neural networks, which include, as special cases, the time-varying delay Hopfield neural networks (HNN), bidirectional associative memory (BAM), and cell neural networks (CNN). The new stability criteria improve upon several results appeared in the literature. To demonstrate the differences and features of the new stability criteria, several examples are discussed.

**Keywords.** Razumikhin technique, Neural networks, Globally exponential stability, Lyapunov exponent, Time-varying delay.

## 1 Introduction

It is well-known that neural networks have been successfully used in associative memories, optimization solvers, signal and image processing, artificial intelligence, and so on. Such applications link heavily with the stability

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