

## STABILITY OF SINGULARLY PERTURBED DIFFERENTIAL-DIFFERENCE SYSTEMS: A LMI APPROACH

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**Abstract.** For linear singularly perturbed system with delay sufficient conditions for stability for all small enough values of singular perturbation parameter  $\varepsilon$  are obtained in the general case, when delay and  $\varepsilon$  are independent. The sufficient delay-dependent conditions are given in terms of linear matrix inequalities (LMIs) by applying an appropriate Lyapunov-Krasovskii functional. LMIs are derived by using a descriptor model transformation and Park's inequality for bounding cross terms. A memoryless state-feedback stabilizing controller is obtained. Solution is given also in the case of systems with polytopic parameter uncertainties. Numerical examples illustrate the effectiveness of the new theory.

**Keywords.** Singular perturbations, time-delay systems, stability, LMI, delay-dependent criteria.

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## 1 Introduction

It is well-known that if the ordinary differential system of equations is asymptotically stable, then this property is robust with respect to small delays (see e.g. [2], [12]). Examples of the systems, where small delays change the stability of the system are given in [13] (see also references therein). All these examples are infinite-dimensional systems, e.g. difference systems, neutral type systems with unstable difference operator or systems of partial differential equations. Another example of a system, sensitive to small delays, is a descriptor system [18]. Recently a new example has been given of a finite dimensional system that may be destabilized by introduction of small delay in the loop [5]. This is a singularly perturbed system. Consider the following simple example:

$$\varepsilon \dot{x}(t) = u(t), \quad u(t) = -x(t-h), \quad (1)$$

where  $x(t) \in R$  and  $\varepsilon > 0$  is a small parameter. Eq. (1) is stable for  $h = 0$ , however for small delays  $h = \varepsilon g$  with  $g > \pi/2$  this system becomes unstable (see e.g. [2]).

Stability of singularly perturbed systems with delays has been studied in two cases: 1)  $h$  is proportional to  $\varepsilon$  and 2)  $\varepsilon$  and  $h$  are independent. The first