

A PROBLEM OF MODAL CONTROL IN A LINEAR NEUTRAL SYSTEM

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Abstract. A problem of modal control is considered for a class of linear multidimensional differential delay systems of neutral type. The control vector is sought in the form that results in a given in advance characteristic equation of the closed system. The problem is completely solved for systems of a special form, the so-called *canonical* systems. A two-dimensional example is considered in full detail.

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1 Introduction

A problem of modal control for linear stationary systems of differential equations without delay of the form

$$\dot{x}(t) = Ax(t) + bu(t), \quad u(t) = c^T x(t), \quad t \geq 0$$

is to find the control parameters $c^T = (c_1, c_2, \dots, c_n)$ that make the characteristic quasi-polynomial

$$\tilde{f}_n(\lambda) = \lambda^n + q_1 \lambda^{n-1} + \dots + q_{n-1} \lambda + q_n$$

of the closed system

$$\dot{x}(t) = (A + bc^T)x(t), \quad t \geq 0$$

to have given in advance zeros $\lambda_1^0, \lambda_2^0, \dots, \lambda_n^0$. Since q_1, q_2, \dots, q_n are uniquely determined from the roots of the characteristic equation, the problem can be stated in terms of a control over the coefficients. This means that one seeks parameters $c_i, i = \overline{1, n}$, such that the characteristic equation of the closed system has given in advance coefficients.